## Advanced Numerical Methods - Homework 1.

## Exercise 1

Give all solutions to the ODE

$$
y^{\prime}=\frac{1}{x} y
$$

## Exercise 2

Solve the initial value problem

$$
y^{\prime}=1+y^{2}, \quad y(0)=0
$$

## Exercise 3

Solve the ODE

$$
y^{\prime}=\frac{1}{x} y+\frac{1}{y} .
$$

and draw different solutions in a diagram. Indicate the corresponding direction field in your drawing as well.
Hint: Substitute $u(x)=\frac{y(x)}{x}$.

